## Model of high-frequency hopping photoconductivity of doped silicon

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A phenomenological model of high-frequency hopping photoconductivity along excited metastable states of an impurity in a semiconductor is developed. Polarization conductivity arises as a result of changes occurring in the dipole moments of pairs of ions of the majority and compensating impurities due to electronic transitions between ionized and excited atoms of the majority impurity in a high-frequency electric field. It is shown that complexes, including excited and ionized atoms of the majority impurity and an ion of the compensating impurity, contribute to the high-frequency hopping conductivity. Such complexes are formed as a result of the capture of photocarriers on dipoles and drift of ions of the majority impurity in the electric field of the ions of the compensating impurity. Simple expressions are obtained for the high-frequency hopping photoconductivity as a function of the excitation intensity, the concentrations of the majority and compensating impurities, and the temperature. Estimates are presented of the absolute magnitude of the high-frequency photoconductivity. The model satisfactorily describes the experimentally established laws of extrinsic photoconductivity of silicon, doped with group III and V impurities, with a microwave bias voltage.

## **1. INTRODUCTION**

In Refs. 1-4 it was established that the kinetics of extrinsic photoconductivity of silicon, doped with a number of group-III and -V elements in concentrations above  $10^{16}$  cm<sup>-3</sup>, under a microwave (37 GHz) bias voltage is determined by two relaxation times—a short relaxation time  $\tau$ ,  $(10^{-8}-10^{-10} \text{ sec})$ , equal to the lifetime of free photocarriers under a constant bias voltage, and a long relaxation time  $\tau^{\ast} \approx 10^{-3}$  sec. Slow relaxation is observed at temperatures  $T \leq 15$  K. When the exciting radiation has a modulation frequency  $f \ll 1/\tau^*$  the high-frequency photoresponse can be almost three orders of magnitude higher at 5 K than the photoresponse with a constant bias voltage. Slow relaxation of extrinsic absorption with time constants close to  $\tau^*$  was observed in the same samples of doped silicon.<sup>3</sup>

The observed phenomena were explained by the existence of metastable excited states of the impurities. The long lifetime of these states causes charge carriers trapped by impurity ions in the process of recombination to accumulate on them. In the present paper we propose a phenomenological model of hopping photoconductivity in which metastable states participate. This model explains the basic laws established by experimental investigations of high-frequency extrinsic photoresponse of doped silicon.<sup>1-4</sup>

Silicon samples doped with boron in concentrations  $N = 10^{15} - 4 \cdot 10^{16}$  cm<sup>-3</sup> and compensated with phosphorus in concentrations  $N_+ = 10^{12} - 10^{14}$  cm<sup>-3</sup>, were studied in greatest detail in Ref. 4. For this reason, we consider a model for the case of a hole semiconductor. In the case of impurity photoexcitation the holes are captured by negatively charged ions of the majority impurity in high excited states,<sup>5</sup> and by emitting and absorbing phonons they relax into a metastable state from which optical transitions into the ground state are forbidden. In the case of boron this can be the  $1S(P_{1/2})$  state with an ionization energy of 23 meV.<sup>6</sup> This state is formed from wave functions of the branch of the valence band that is split off by the spin-orbital interaction. Under quasisteady excitation conditions the ratio of the con-

centration of free nonequilibrium holes to the concentration  $N_{\star}$  of localized nonequilibrium holes should be equal to  $\tau_r/$  $\tau^*$ , i.e., it should reach 5–7 orders of magnitude for the silicon samples investigated. This difference is apparently insufficient for hopping photoconductivity to predominate over photohole photoconductivity under a constant bias voltage. When a high-frequency bias is voltage is applied, however, polarization conductivity should appear.<sup>7</sup> Polarization conductivity appears as a result of a change in the dipole moments of the pairs of ions of the majority and compensating impurities in an electric field. In order to magnitude the time constant of this change is equal to the hopping time  $\tau$ between ionized and neutral atoms of the majority impurity, and the total change in the polarization of the semiconductor in an alternating electric field with frequency  $\omega$  is manifested as flow of an alternating current. In this case the dark ac conductivity is many orders of magnitude greater than the dc conductivity.7 In the case of extrinsic photoexcitation the excited metastable states of atoms of the majority impurity with large Bohr radii a\* are included in the process, and this should strongly increase the polarization hopping conductivity.

## 2. PHENOMENOLOGICAL MODEL

Holes accumulate in metastable states as a result of being captured by both isolated ions with concentration  $N_{-}$ and dipoles with concentration  $N_{+-}$  (Ref. 5). In the case of capture by dipoles the excited atoms are localized near ions of the compensating impurity at a characteristic distance  $r_{av} = (4\pi N/3)^{-1/3}$ , forming positively charged pairs with concentrations  $N_{+*}$ . When the frequency  $\omega = 2.3 \cdot 10^{11}$ sec<sup>-1</sup> of the ac electric field is high (Refs. 1-4), only hops between close ionized and excited atoms can contribute to the hopping conductivity  $\sigma(\omega)$ . Since both photoionization and capture are random processes, the probability of formation of such close pairs is small if the degree of excitation is low. However, the electrostatic attraction between isolated ions  $N_{-}$  and pairs  $N_{+*}$  should draw them together and re-

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sult in the formation of complexes in concentrations  $N_{+*}$ , consisting of excited and ionized atoms of the majority impurity and an ion of the compensating impurity. The average distance between all partners in such complexes will also be close to  $r_{av}$ , determined by the concentration of the majority impurity N. It is these complexes that should make the main contribution to the polarization hopping conductivity.

The fraction of excited atoms localized near ions of the compensating impurity is determined by the distribution of the recombination fluxes of holes between ions and dipoles, and is equal to

$$C = \frac{\alpha_{+-}N_{+-}}{\alpha_{+-}N_{+-} + \alpha_{-}N_{-}},$$
 (1)

where  $\alpha_{-}$  and  $\alpha_{+-}$  are the hole capture coefficients of ions and dipoles, respectively. Note that  $N_{-}$  is the total concentration of isolated ions of the majority impurity, which appear with thermal and optical excitation, including also holes captured by neutral acceptors with consequent formation of  $A^+$  centers.<sup>8</sup> If the nearest negatively charged ion of the majority impurity is located at a distance R when  $N_{+*}$ pair is created, then it is drawn to the pair over the drift time

$$t_d = \frac{\varepsilon R^3}{3e\mu_h},\tag{2}$$

where e is the electron charge,  $\varepsilon$  is the dielectric permittivity, and  $\mu_h$  is the hopping "mobility." The number of such ions in a spherical shell (R, R + dR) is

$$dN_{-} = N_{-} \cdot 4\pi R^2 \exp(-R/R_{\rm av})^3 dR , \qquad (3)$$

where  $R_c = (\frac{4}{3} \cdot \pi \cdot N_-)^{-1/3}$ . Since the excitation relaxes as  $\exp(-t/\tau^*)$ , complexes are formed efficiently only if  $t_d < \tau^*$ . For this reason the concentration  $dN_{+*-}$  of complexes formed as a result of drift of ions  $N_-$  to pairs  $N_{+*}$  from a distance R is

$$dN_{+*-} = N_* C \exp(-t_d/\tau^*) dN_-.$$
(4)

In the case of steady excitation with rate G we have  $N_* = G\tau^*$ . Integrating Eq. (4) over all values of R, substituting Eqs. (1)-(3), we obtain

$$N_{+*-} = CG\tau^* (1 + \tau_M / \tau^*)^{-1} , \qquad (5)$$

where  $\tau_M = \varepsilon/4\pi\sigma_h$  is the Maxwellian relaxation time of the charge due to hopping conductivity  $\sigma_h = e\mu_h N_-$ .

In the case of impulsive excitation with duration  $\Delta t$ , when  $\tau_r \ll \Delta t \ll \tau^*$  only ions  $N_-$  which were able to traverse a distance  $R_d = (3e\mu_h t/\varepsilon)^{1/3}$  over the time  $t_d$  will participate in the photoconductivity. Hence

$$N_{+*-} = CG\Delta t \exp\left(-\frac{t}{\tau^*}\right) \int_0^{R_d} 4\pi R^2 \exp\left(-\frac{R}{R_{\rm av}}\right)^3 dR$$
(6)

or

$$N_{+*-} = CG\Delta t \exp(-t/\tau^*) [1 - \exp(-t/\tau_M)] .$$
 (7)

The conductivity  $\sigma(\omega)$  can be determined using the expressions obtained in Ref. 7 for polarization hopping conductivity, replacing the dipole concentration in them, which is equal to the concentration  $N_+$  of the compensating impu-

rity, by the concentration  $N_{+*}$  – of complexes from Eq. (5) or (7). Then according to Ref. 7, in an electric field with frequency  $\omega$  the contribution to  $\sigma(\omega)$  of electronic transitions between excited and ionized atoms of the majority impurity, which are located at a distance *r* from one another, in which the energy changes by  $\Delta E$  in a hop, is

$$d\sigma(r,\,\omega,\,\Delta E) = \frac{N_{+*-}e^2r^2}{12kT\tau} \left(\frac{\omega^2\tau^2 + i\omega\tau}{1+\omega^2\tau^2}\right) \frac{dN}{\mathrm{ch}^2(\Delta E/2kT)},$$
(8)

where  $dN = 4\pi \cdot Nr^2 dr$ , and the hopping time is determined by the relation

$$\tau \approx 5 \cdot 10^{-13} \left(\frac{r}{a^*}\right)^{-3/2} \exp\left(\frac{2r}{a^*}\right) \operatorname{th}\left(\frac{\Delta E}{2kT}\right) \,. \tag{9}$$

At the frequency  $\omega = 2.3 \cdot 10^{11} \text{ sec}^{-1}$  the condition  $\omega \tau > 1$  is satisfied essentially up to  $r = a^*$ . For this reason, in Eq. (8) the real part of the photoconductivity is much larger than the imaginary part, and the frequency dependence  $\sigma(\omega)$  can be neglected. However, the change  $\Delta E$  in the energy of a dipole accompanying a hop can be significant, since the hopping length is of the same order of magnitude as the distance  $r_{av} = (4\pi N/3)^{-1/3}$  between an ion of the compensating impurity and the atom of the majority impurity, and  $\Delta E/kT$  cannot be considered small at low temperatures. Including in Eqs. (8) the functional dependence of  $\Delta E$  on the hopping length and the direction of a hop with respect to the arm of the dipole is an unwarranted complication of the problem. For this reason, we employ the following rough approximation to estimate the absolute value of  $\sigma(\omega)$ .

We assume that both the average distance between the ions of the majority and compensating impurities and the averaging hopping length are close to  $r_{\rm av}$ . Then only hops with  $\Delta E \leqslant kT$  occur. The fraction of hops in directions for which this condition is satisfied is approximately  $kT/E_c$ , where  $E_{\rm av} = e^2/\epsilon r_{\rm av}$ . Then in expressions (8) and (9) we can set  $\cosh^2(\Delta/2kT) \times \tanh(\Delta E/2kT) = 0.5 \cdot \sinh(\Delta E/kT) < 1/2$ , and the expression (8) becomes

$$d\sigma(\omega, r) = \frac{N_{+*-}e^{2r^2(r/a^*)^{3/2}\exp(-2r/a^*)dN}}{5 \cdot 10^{-13} \cdot 6E_{av}},$$
 (10)

which, after integrating over r, gives

$$\sigma(\omega) = \frac{N_{++-}}{2r_{\rm av}^2} \frac{\varepsilon}{5 \cdot 10^{-13}} \left(\frac{a^*}{2}\right)^5 \frac{\Gamma(13/2)}{2^{13/2}}.$$
 (11)

## **3. COMPARISON WITH EXPERIMENT**

According to expression (11), the dependence of the quasistationary polarization photoconductivity  $\sigma(\omega)$  on the degree of excitation and the concentrations of the majority and compensating impurities is determined by the concentration  $N_{+*-}$  of the complexes, given by (5).

In Ref. 4 it was established experimentally that, in agreement with Eq. (5), the quasistationary photoresponse in a microwave electric field  $U_{\rm LF} \propto \sigma(\omega)$  is a linear function of the excitation rate G. Such a linear relation should hold only for  $N_{\star} < N_{+}$ . When, however, an excited and an ion-

ized atom of the majority impurity are present near each ion of the compensating impurity, further increase of excitation should not cause  $\sigma(\omega)$  to increase. Indeed, in Ref. 4 the photoresponse was observed to saturate for  $G\tau^* \ge N_+$ .

The dependence of  $U_{\rm LF}$  on the concentration  $N_+$  of the compensating donors is determined by the parameter C given by Eq. (1). This parameter describes the distribution of recombination fluxes between dipoles and isolated ions of the majority impurity. As shown in Ref. 5 and 9, at low temperature under conditions of thermodynamic equilibrium with a fixed concentration of the majority impurity the dipole concentration  $N_{+-}$  decreases as the concentration  $N_+$  of the compensating impurity decreases. Using the results of Refs. 5 and 9, we calculated for the concentrations  $N = 3.5 \cdot 10^{16} \, {\rm cm}^{-3}$  and  $N_+ = 2 \cdot 10^{12} - 10^{14} \, {\rm cm}^{-3}$  and T = 5 K the parameter C for different values of the ratio  $\alpha_-/\alpha_{+-}$ .

Figure 1 displays the parameter C calculated in this manner as a function of  $N_+$ , the dependence being extremely strong  $[\alpha_{-}/\alpha_{+-} = 60]$  for the indicated range of concentrations of the compensating donors. The figure also displays the experimental dependence<sup>4</sup> of the photoresponse  $U_{\rm LF}$  on the concentration  $N_+$ . When the boron concentration is  $N = 3.5 \cdot 10^{16}$  cm<sup>-3</sup>. It is evident from the figure that we have  $U_{\rm LF} \propto N_+$ , although the calculation for thermodynamically equilibrium conditions gives a much weaker dependence. This discrepancy is due to the strong departure from equilibrium under the conditions of the experiment, thanks to which  $N_{+-}$  and  $N_{-}$  are determined not only by N,  $N_{\perp}$ , and the temperature, but also by the background illumination, which was neglected in Ref. 5. This leads, in particular, to the formation of A<sup>+</sup> centers<sup>8</sup> and an increase in the concentration  $N_{-}$  of the charge compensating them. For this reason, in order to determine the parameter C we employ the experimental  $U_{\rm HF}$  dependence of the microwave photoresponse at high modulation frequency of the exciting radiation  $1/\tau^* \ll 2\pi f < 1/\tau_r$ . We take into account the fact that  $U_{\rm HF} \propto \sigma(0)$ , i.e., it is proportional to the quasistationary photoconductivity with constant bias voltage.<sup>1,2,4</sup> In comparatively weakly compensated samples we have  $N_+ \ll N$ , and the mobility  $\mu_p$  of free holes is determined by scattering by neutral impurities. For this reason  $U_{\rm HF} \propto [\alpha_{-}N_{-} + \alpha_{+}N_{+}]^{-1}$  holds. At high temperatures  $T \ge 25$  K the hole recombination flux on dipoles can be neglected and  $U_{\rm HF} \propto [\alpha_- N_-]^{-1}$ . For a sample with minimum concentration  $N_+ = 2 \cdot 10^{12}$  cm<sup>-3</sup> the rate of capture on dipoles,  $\alpha_+ \_ N_+ \_$ , calculated for the case of thermodynamic equilibrium according to Refs. 5 and 9, is negligibly small compared with  $\alpha_- N_-$  at all temperatures down to 5 K, i.e., for this "reference" sample  $U_{\rm HF}^0 \propto [\alpha_- N_-]^{-1}$  $= [\alpha_- N_+]^{-1}$ . Then the discrepancy appearing between the dependences  $U_{\rm HF}$  and  $U_{\rm HF}^0$  as the temperature decreases is caused by the fact that dipoles with concentration  $N_{+-}$  in the samples with high compensation are engaged in the capture process. Matching the plots of  $U_{\rm HF}$  for each sample with the reference plot  $U_{\rm HF}^0$  at high temperatures (25–30 K), we can determine the fraction of the recombination flux on dipoles directly from Fig. 2 at any temperature

$$C = \frac{\alpha_{+-}/\alpha_{-}}{1 - \alpha_{+-}/\alpha_{-}} \left( \frac{U_{\rm HF}}{U_{\rm HF}^{0}} - 1 \right).$$
(12)

Figure 1 displays the parameter C determined as a function of  $N_{+}$  at 5 K by means of the procedure described above. It is evident that this relation is nearly linear, i.e., it agrees with the relation established in Ref. 4. We note that the temperature dependence of  $U_{\rm HF}^{0}$  differs insignificantly from the temperature dependence of  $\tau_r$ , calculated in Ref. 5 neglecting the formation of dipoles. As the temperature increases, the dipoles dissociate, and this results in a decrease of  $U_{\rm LF}$ . The temperature dependences of  $U_{\rm LF}$  in Fig. 2 are plotted so that for different samples they coincide at high temperatures. It is evident that the hopping photoconductivity  $U_{\rm LF}$  starts to exceed the photoconductivity due to free holes  $U_{\rm HF}$  precisely at the temperatures when capture of holes on dipoles starts to play a significant role, i.e., when the temperature dependence of  $U_{\rm HF}$  and of  $U_{\rm HF}^0$  disagree. This confirms the initial assumption that the microwave hopping photoconductivity is connected with capture of photoholes on dipoles. At high concentrations of the majority and compensating impurities capture on dipoles predominates up to 15 K, and as the temperature increases further the decrease of  $U_{\rm LF}$  is determined by thermal ionization of the metastable state with activation energy close to 23 meV (Ref. 4).

In Ref. 4 it was established that at low temperatures the



U<sub>LF</sub>, arbitrary units

FIG. 1. Relative photoresponse at low modulation frequency  $U_{\rm LF}$ , of the exciting radiation, according to Ref. 4 ( $\oplus$ ), and relative value of the parameter  $C = U_{\rm HF}/U_{\rm HF}^0$  – 1 ( $\Box$ ), as functions of the concentration of compensating donors  $N_+$  in samples with the boron concentration  $N = 3.5 \cdot 10^{16}$  cm<sup>-3</sup> at 5 K; the dashed line represents the curve of C calculated according to Refs. 5 and 9 for  $\alpha_-/\alpha_{+-} = 60$ .



FIG. 2. Temperature dependence of the relative photoresponse with low  $U_{\rm LF}$  (solid lines) and with high  $U_{\rm HF}$ (dashed lines) modulation frequency of the exciting radiation for samples with boron concentration  $N = 3.5 \cdot 10^{16}$ cm<sup>-3</sup> and concentration of compensating donors (cm<sup>-3</sup>)

photoresponse  $U_{\rm LF}$  with fixed concentration of  $N_+$  of compensating donors ( $N_+ = 10^{14} {\rm cm}^{-3}$ ) is virtually independent of the concentration of the majority impurity (boron) for  $N \ge 2.7 \cdot 10^{16} {\rm cm}^{-3}$ , but at lower concentrations

$$U_{\rm LF} \propto \exp(-r_{\rm av}/r_0), \qquad (13)$$

where the optimal value is  $r_0 = 1.7 \cdot 10^{-7}$  cm. According to the expression (5), the weak dependence of  $\sigma(\omega)$  on N should be observed until  $\varepsilon/4\pi\sigma_h = \tau_M < \tau^*$ . At  $\tau^* = 5 \cdot 10^{-4}$  sec this corresponds to a hopping conductivity  $\sigma_h = 2 \cdot 10^{-8} \ (\Omega \cdot \text{cm})^{-1}$  in a constant electric field. In the experiment of Ref. 4 the samples were illuminated with constant background illumination, which determined their conductivity. The free holes and the hopping mechanism made comparable contributions of the conductivity. At 5 K the conductivity of silicon samples with  $N = (2.7-4) \cdot 10^{16}$ cm<sup>-3</sup> was at least  $10^{-7}$  ( $\Omega \cdot$  cm)<sup>-1</sup>, i.e., it exceeded the indicated critical value. The exponential drop in  $U_{\rm LF}$  for  $N < 2.7 \cdot 10^{16}$  cm<sup>-3</sup>, which we attribute to the exponential decrease of  $\sigma_h$ , should satisfy the relation  $\sigma_h$  $\propto \exp(-2.78r_{\rm av}/a)$  established for the hopping conductivity,<sup>10</sup> where  $a = 2.2 \cdot 10^{-7}$  cm is the Bohr radius of the ground state of the acceptor. For  $r_0 = 1.7 \cdot 10^{-7}$  cm, however, we must set  $a = 4.7 \cdot 10^{-7}$  cm in Eq. (13), which is approximately twice the Bohr radius. This discrepancy could arise for the following reasons. First, the coefficient 2.78 in the expression for  $\sigma_h$  was obtained in Ref. 10 in a calculation of charge transfer along an infinitely long chain of impurities (an infinite cluster). In our model the  $N_{-}$  ions drift toward the positively charged  $N_{\perp}$  donors through atoms of the majority impurity, which form clusters of finite size less than  $N_{+}^{1/3} \leq 10^{-4}$  cm. The conductivity of some clusters is significantly higher than the average equilibrium conductivity  $\sigma_h$ . For this reason, averaging over an ensemble of independent clusters can weaken the exponential dependence of  $\sigma_h$  on  $r_{av}$ . Second, we must include the fact that the ions  $N_{-}$  drift in the electric field produced by the ions

 $N_+$ , which for  $R \le 10^{-5}$  cm is greater than 100 V/cm and is not weak.<sup>11</sup> For this reason, the drift velocity may be higher than expected, which will also weaken the concentration dependence of  $U_{\rm LF}$ . On the basis of these remarks, it should be noted that both the transition to the exponential dependence of  $U_{\rm LF}$  with  $\tau_M \approx \tau^*$  and the value of  $r_0$  in Eq. (13), in our opinion, support the proposed model.

We now estimate the absolute magnitude of the lowfrequency hopping photoconductivity for a strongly doped sample with boron concentration  $N = 4 \cdot 10^{16}$  cm<sup>-3</sup> and  $N_{+} = 10^{14} \text{ cm}^{-3} \text{ at } 5 \text{ K}$ , setting C = 1,  $\varepsilon = 12$ ,  $\tau^* = 5 \cdot 10^{-4}$  sec, and  $a^* \approx 2a \approx 4 \cdot 10^{-7}$  cm. Substituting these values into Eq. (5), we obtain  $U_{\rm LF} \propto \sigma(\omega) \approx 2 \cdot 10^{-24} G(\Omega \cdot {\rm cm}^{-1})$ . For photoconductivity due to free holes in such a sample we can set  $\tau_r = 10^{-10}$  sec and take the mobility to be  $\mu_p = 10^4 \,\mathrm{cm^2}/$ V·sec, whence  $U_{\rm HF} \propto \sigma(0) = Ge\mu_r \tau_r$ =  $1.6 \cdot 10^{-25} G(\Omega \cdot \text{cm})^{-1}$ . Hence  $U_{\text{LF}} / U_{\text{HF}} \approx 10$ . The experimental value of the ratio  $U_{\rm LF}/U_{\rm HF}$  is at least an order of magnitude larger.<sup>4</sup> In view of the roughness of the estimate presented, and primarily the possible uncertainty in calculating the hopping time  $\tau$  and taking into account the change  $\Delta E$  in the dipole energy accompanying a hop, this discrepancy is not in conflict with the proposed model.

In Refs. 12 and 13 a theory of hopping photoconductivity in a system with localized states was developed for the case when the equilibrium state is reached due to diffusion of localized charge carriers, but the possibility of charges of different signs drifting toward one another was neglected. Taking this into account in the case of a doped and partially compensated semiconductor seems to us to be the key to analyzing hopping photoconductivity. The proposed model of hopping photoconductivity along excited metastable states of impurities in silicon agrees, at least qualitatively, with experiment.<sup>1-4</sup> The quantitative discrepancies could be connected with the strong departure of the electronic system equilibrium, unavoidable under experimental conditions. Attractive features of the model are the physically clear mechanism by which the excited and ionized atoms of the majority impurity approach one another, i.e., the drift of the ionized atoms in the electric field generated by the ions of the compensating impurity, and the possibility of restoring a stationary state due to the hopping mechanism of transfer of the ion charge.<sup>5</sup>

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