## Direct-capture threshold effects in silicon superconductivity

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The photoconductivity (PC) of silicon with degree of compensation  $K < 10^{-3}$  and with mainimpurity density N exceeding somewhat the delocalization threshold of the  $D^-$  states was experimentally investigated at helium temperatures (T) and in various electric fields (E). An abrupt PC threshold ( $\sigma_g$ ) was observed in the  $D^-$  band for samples with  $K > 10^{-4}$  at  $T > T_{cr}$ (or  $E > E_{cr}$ ). The effect on E on the free-carrier conductivity ( $\sigma_c$ ) turned out to be stronger the higher T. The results are explained using the indirect-recombination method. It is shown that the second recombination stage, carrier capture from the  $D^-$  band by an attracting center (AC) can be represented as carrier drift toward the AC under the influence of the Coulomb field of the latter. The threshold of the onset of the conductivity  $\sigma_g$  is explained. Estimates of  $T_{cr}$ , of  $E_{cr}$ , and of the coefficient of carrier capture by the AC from the  $D^-$  band are explained. The values obtained on the basis of this model are close to those obtained in experiment.

## **1. INTRODUCTION**

We have shown earlier<sup>1,2</sup> that the  $D^{-}$  states influence substantially at helium temperatures the photoconductivity (PC) in doped silicon  $(N > 10^{16} \text{ cm}^{-3})$  with very small compensation ( $K \leq 10^{-3}$ ). According to Refs. 1 and 2, the recombination of free electrons with attracting centers (AC) is effected at  $K \leq 10^{-3}$  in two stages (indirect recombination): the electron is first captured by a neutral center (NC) and then goes over from the NC to the AC. For small N and "large"  $K(N < 2 \cdot 10^{16} \text{ cm}^{-3}, K \ge 10^{-4})$  the number of NC participating in the recombination is relatively small; their distance R from the AC does not exceed a certain value  $R_{\rm eff}(T)$ . The second stage is in this case a hopping approach of the electron to the AC. The NC located at a distance  $R > R_{eff}$  from the AC take no part in the recombination and act as sticking centers. At large N and small  $K(N > 4 \cdot 10^{16} \text{ cm}^{-3}, K \le 10^{-4})$  the D<sup>-</sup> states are in the main already delocalized. The second recombination state is therefore effected by electron motion over the  $D^{-}$  band and an appreciable fraction of the NC participate in the recombination. A distinguishing feature of such samples is the possible appearance in the  $D^-$  band of a photoconductivity (PC)  $\sigma_{\rm g}$  that can be comparable with or even larger than the PC  $\sigma_c$  in the free band (c band).

The above division of samples into two groups is to a certain degree arbitrary.<sup>2</sup> In some intermediate samples the physical situation is different, depending on the temperature T and on the electric field E. The present paper is devoted to the properties of such samples. Principal attention is paid to the investigation of the conditions under which  $\sigma_g$  sets in when T, E, and K are varied, and also of the dependences of  $\sigma_g$  and  $\sigma_c$  on these quantities.

Our most important results can be formulated as follows: Samples exist in which the conductivity  $\sigma_g$  is zero at small T and E but increases when they increase. It has turned out that the onset of  $\sigma_g$  has a threshold—it appears almost jumpwise at a certain  $T = T_{cr}$  or  $E = E_{cr}$ . The field dependences of  $\sigma_c$  are radically different from those in cascade capture: the effect of E on  $\sigma_c$  is weaker the lower T. We were able to explain the results using an indirectrecombination model. The heretofore ignored capture of  $D^-$ -band electrons by AC can be regarded as electron drift to the AC by the action of the Coulomb field of the center. The jumplike onset of  $\sigma_{g_1}$  and the unusual behavior of  $\sigma_c(T,E)$  are explained by this model. The coefficient  $\alpha_g^+$  of capture of a  $D^-$ -band electron by an AC and the values of  $T_{cr}$  and  $E_{cr}$  are estimated without using any adjustment parameters. The values obtained for  $\sigma_g^+$ ,  $T_{cr}$ , and  $E_{cr}$  have turned out to be close to the measured ones.

## 2. EXPERIMENTAL PROCEDURE AND RESULTS

We investigated a set of Si:B samples with  $n = (2 - 1)^{n}$ 12)  $\cdot 10^{16}$  cm<sup>-3</sup> and  $K = 10^{-5} - 10^{-3}$ . The free carriers were photoexcited by background radiation at room temperature in a photon energy range  $\hbar\omega = 80-120$  meV (interference filter). The excitation intensity  $(W_{\rm ph}N)$  was relatively low  $(W_{\rm ph} \simeq 0.1 - 1 \text{ s}^{-1})$ . We measured the conductivity  $\sigma$  and the Hall constant  $R_H$ . At  $\mu^* \equiv R_H \sigma \simeq \mu_c$ , where  $\mu_c$  is the free-carrier mobility, the conduction was only via the c-band (all the reasoning that follows pertains to *n*-type material):  $\sigma = \sigma_c$ . At  $\mu^* < \mu_c$  a contribution is made by conduction through the D  $^-$  band:  $\sigma = \sigma_c + \sigma_g$ . In this case  $\sigma_c$  and  $\sigma_g$ were calculated using the two-band model (see Ref. 3 for more details). Under the experimental conditions the mobility  $\mu_c$  was determined by scattering from neutral impurities:  $\mu_c(E,T) = \mu_n = \text{const.}$  The shown measurement results for two most typical samples are representative of the large batch.

Figures 1 and 2 show the temperature dependences of  $\sigma_c$  and  $\sigma_g$  for samples  $1(N \simeq 6 \cdot 10^{16} \text{ cm}^{-3}, KN \approx 4 \cdot 10^{13} \text{ cm}^{-3})$  and  $2(N \simeq 6 \cdot 10^{16} \text{ cm}^{-3}, KN \approx 6 \cdot 10^{12} \text{ cm}^{-3})$  for different *E*. Three sections can be distinguished on the  $\sigma_c(T)$  curves; low  $T(T < T_2) - \sigma_c = \text{const}$ , intermediate  $(T_2 < T < T_1) - \sigma_c(T) \propto \exp(-\varepsilon_x/kT)$ , and high  $(T > T_1) - \sigma_c(T) \propto T^{2.5}$ . As *E* increases the  $\sigma_c$  curves undergo a certain evolution:  $T_2$  decreases and  $T_1$  increases, i.e., the intermediate-temperature region broadens. For sample 1



FIG. 1. Dependences of  $\sigma_c(T)$  and  $\sigma_g(T)$  (numbers of primed curves) for sample 1 at different values of E(V/cm):1-5; 2,2'-40; 3,3'-60, 4,4'-80. Dashed curves—dependences of  $\sigma_g(T) \propto T^2$ . Curve 5—calculated dependence of  $x_T(T)$ ; curve 6—dependence of  $\sigma_g(T)/x_T(T)$  for curve 2'.

at E = 5 V/cm this region is nonexistent,  $T_1 \le T_2$ , and no  $\sigma_g$ is observed. At E = 40 V/cm the conductivity  $\sigma_g$  is zero up to a certain critical temperature  $T_{cr} \simeq 2.8$  K, after which  $\sigma_g(T)$  is seen to grow abruptly. At  $T \simeq 5$  K the value of  $\sigma_g$  is already comparable with  $\sigma_c$  and increases smoothly with further increase of T. The  $\sigma_g(T)$  dependence becomes weaker when E increases at low T. At intermediate T we have  $\sigma_g(T) \sim T^2$ , after which  $\sigma_g$  has a maximum. The temperature corresponding to the maximum of  $\sigma_g(T)$  is higher the larger E. In sample 2 the conductivity  $\sigma_g$  exists in all fields, while in a field 10 V/cm the increasing  $\sigma_g$  also has a threshold at  $T = T_{cr} \le 2$  K. Note that  $\sigma_g$  increases with decrease of  $NK \equiv N^+$  (it follows from measurements of sample batches that  $\sigma_g \sim 1/N^+$  for equal T and E).

Figure 3a shows a plot of  $\sigma_c(E)$  for sample 2 at various



FIG. 2. Dependences of  $\sigma_c(T)$  and  $\sigma_g(T)$  (numbers of primed curves) for sample 2 at different values of E(V/cm): 1---10; 2---20; 3---60; 4---100. Dashed curves-dependences of  $\sigma_g(T) \propto T^2$ .

T. Evidently, the  $\sigma_c(E)$  dependence becomes stronger with increase of T. We emphasize that this fact is not at all understandable in light of the usual assumptions concerning the heating and capture of electrons. Figure 3b shows the  $\sigma_g(E)$ dependence for samples 1 (curve 7) and 2 (curves 5 and 6). In sample 1,  $\sigma_g$  is zero up to a certain critical value  $E_{\rm cr} \simeq 30$ V/cm, where it rises above a threshold. In sample 2  $\sigma_g$  increases monotonically with the field. The  $\sigma_g$  dependence weakens when the temperature is raised.

## **3. DISCUSSION OF RESULTS**

Let us show that the dependences of  $\sigma_g$  and  $\sigma_c$  on T and E can be explained using the indirect recombination mech-



FIG. 3. a) Dependences of  $\sigma_c(E)$  for sample 2 at 1— T = 2 K; 2—4.2 K; 3—6 K; 4—10 K. b) Dependences of  $\sigma_g(E)$  for sample 1 at 5—T = 2.5 K; 6—4.2 K. Curve 7 dependence of  $\sigma_g(E)$  for sample 1 at T = 2.5 K; junction with curve 5 at E = 100 V/cm. Curve 8—calculated dependence of  $x_E(E)$ . Curve 9 (dashed)—dependence of  $\sigma_g(E)/x_E(E)$  for curve 7.

anism proposed by us earlier,  $^{1,2}$  if it is assumed that  $D^{-}$ -band electron recombination on an AC is the result of directed motion of these electrons to the AC in its Coulomb field.

1. Consider the dependence of  $\sigma_c$  on E and T. The increase of  $\sigma_c$  with E is due to the increased density  $n_c$  of the free electrons as the lifetime increases  $[\mu_c(E) = \text{const!}]$ .

It was shown in Refs. 1 and 2 that under the considered conditions  $\sigma_c$  cannot be attributed to cascade capture by an AC. One more argument must be added to the statements there. We have already emphasized that the  $\sigma_c(E)$  dependence increases with T. This dependence becomes weaker in cascade capture.

The  $\sigma_c(T)$  dependences are attributed in Ref. 2 to indirect recombination for two limiting cases (see the Introduction): small N and large K ( $K \ge 10^{-4}$ ), and large N and small K ( $K \le 10^{-4}$ ). The lifetime  $\tau_{cl}$  of the free electrons takes in the first of these cases the form<sup>2</sup>

$$\tau_{\rm cl}^{-1} = (4\pi/3) R_{\rm eff}^3 N^+ \tau_n^{-1} \xi \propto T^{-2,5} , \qquad (1)$$

where  $\xi \simeq 1$ ,  $\tau_n^{-1} = \alpha^0 N$ , and  $\alpha^0$  is the coefficient of capture by an NC. In the second case  $(K < 10^{-4})$  an appreciable fraction of the NC takes part in the recombination. An electron trapped on an NC far from an AC contributes to the conductivity through the  $D^-$  band until it is captured by an AC (capture probability  $\alpha_g^+ N^+ = 1/\tau_g^+$ ) or is thermal ejected to the c band (ejection probability  $W_T = \alpha^0 N_c \exp(-\varepsilon_x/kT)$ ,  $N_c$  is the c-band,  $\varepsilon_x$  is the energy gap between the c-band bottom and the maximum of the  $D^-$ -band electron distribution). The corresponding lifetime  $\tau_{c2}$  is

$$\tau_{c2}^{-1} = \tau_n^{-1} (1 + W_T \tau_g^+)^{-1}.$$
(2)

Our samples are intermediate with respect to N and K. Depending on the external conditions (T,E) the main transport of a trapped electron to an AC in the samples can be effected by either method. A somewhat simplified expression for  $\tau_c$  is

$$\tau_{c}^{-1} = \tau_{c1}^{-1} + \tau_{c2}^{-1} = \tau_{c1}^{-1} + \tau_{n}^{-1} (1 + W_{T} \tau_{g}^{+})^{-1}.$$
 (3)

We shall analyze this equation assuming that  $\tau_{c1} \ge \tau_n$ : owing to the very small K this inequality holds for all the employed samples.  $W_T$  increases exponentially with T, the values of  $\tau_{c1}$  and  $\tau_g^{(+)}$  have power-law growth rates, and  $\tau_n$ is independent of T. We denote the temperatures at which  $W_T \tau_g^+ = 1$  and  $W_T \tau_g^+ = \tau_{c1}/\tau_n$ , by  $T_2$  and  $T_1$  respectively. Obviously,  $T_2 < T_1$ , since  $\tau_{c1} \ge \tau_n$ . If  $T < T_1$  we can neglect the first term of (3). The number 1 can be neglected in the denominator of the second term if  $T < T_2$ , and must be retained if  $T > T_2$ . If, however,  $T > T_1$ , the second term of (3) should be omitted. The  $\sigma_c(T) \propto \tau_c(T)$  dependence takes as a result the form

$$\sigma_{c} \propto \tau_{n} = \operatorname{const}(T),$$
  

$$\sigma_{c} \propto \tau_{n} \tau_{g}^{+} W_{T} \propto \exp(-\varepsilon_{x}/kT),$$
  

$$\sigma_{c} \propto \tau_{c1} \propto T^{2,5}$$
(4)

for the three temperature regions  $T < T_2$ ,  $T_2 < T < T_1$  and  $T > T_1$  respectively.

We see that the qualitative results that follow from the analysis of Eq. (3) are fully valid: all three characteristic regions are observed in experiments. This casts light on the physical meanings of the temperatures  $T_1$  and  $T_2$  introduced

in the discussion of Figs. 1 and 2. Expressions (4) describe correctly the  $\sigma_c(T)$  dependence in the entire temperature interval. The quantitative estimates of  $\sigma_c$  yield quite reasonable values.<sup>2</sup>

2. We use now the same model to analyze  $\sigma_g$ , supplementing it with ideas concerning capture of  $D^{-}$ -band electrons by AC.

From the kinetic equations we obtain for the lifetime  $\sigma_g$  in the  $D^-$  band

$$1/\tau_g = 1/\tau_g^{+} + (1 + W_T \tau_g^{+}) \tau_n / \tau_{ci} \tau_g^{+}.$$
 (5)

We assume that the change of  $\sigma_g$  is due mainly to the change of the electron density  $n_g$  in the  $D^-$  band. Since  $n_g \propto \tau_g$ , the  $\sigma_g(T)$  dependence should have two characteristic regions:

$$\sigma_{g} \propto \tau_{g}^{+} \quad (T < T_{1}),$$

$$\sigma_{g} \propto \tau_{c1} / \tau_{n} W_{T} \quad (T > T_{1}).$$
(6)

In the last case  $\sigma_g$  decreases with increase of T in view of the depletion of the  $D^-$  band by thermal ejection of electrons into the c band. Experiment confirms the presence of the two regions: It is seen from Figs. 1 and 2 that near  $T = T_1$  the  $\sigma_g(T)$  dependence changes: the increase of  $\sigma_g$  due to the increase of  $\tau_g^+$  with T (see below) is replaced by a decrease.

3. Let us discuss the field dependences. The electric field deforms the Coulomb potential well. Just as in cascade capture, this deformation decreases the probability of capture by AC and lengthens the times  $\tau_g^+$  and  $\tau_{c1}$ . Thus, the conductivity  $\sigma_g$  should increase with *E*, as is in fact the case.

Turning to Eqs. (4), we conclude that the conductivity  $\sigma_c$  should not depend on E at  $T < T_2$  and should increase with E at  $T \ge T_2$ . This is precisely what is observed in experiment. This explains also the enhancement of the  $\sigma_c(T)$  dependence with increase of T. Thermal excitation causes the  $D^-$  band to supply electrons to the c-band. The increase of  $n_g$  with the field causes therefore  $n_c$  to increase, and more strongly the higher the temperature.

It can be seen from Figs. 1 and 2 that  $T_2$  decreases somewhat with increase of E. This is understandable: the condition  $W_T \tau_g^+ > 1$  is easier to satisfy the longer  $\tau_g^+$ . The temperature  $T_1$  determined by the condition  $\tau_{c1} = \tau_n W_T \tau_g^+$ , increases with E. It can apparently be concluded from this that when E increases  $\tau_{c1}$  increases faster than  $\tau_g^+$ .

Curve 1 of Fig. 1 has no regions of intermediate T. It can be seen that for this sample, in a field 5 V/cm, the first term of (3) becomes predominant when T is increased precisely when the inequality  $W_T \tau_g^+ > 1$  begins to be satisfied.

It is thus possible to understand fully our experimental results from the standpoint of an indirect recombination mechanism if it assumes that  $\tau_g^+$  increases with increase of E. This assumption is intuitively quite reasonable. An estimate of  $\tau_g^+$  can be obtained by starting from the condition  $W_T(T_2)\tau_g^+ = 1$ . For curve 3 of Fig. 2 we have  $\varepsilon_x \simeq 2.75$  meV and  $T_2 \simeq 4$  K. Using for  $N_c$  the density of states in the valence band of silicon ( $\approx 2 \cdot 10^{15} \ T^{3/2} \ cm^{-3}$ ) and  $\alpha^0 \approx 10^{-7} \ cm^3 \cdot s^{-1}$  (Ref. 2) we obtain  $1/\tau_g^+ \approx 6 \cdot 10^5 \ s^{-1}$ . For curve 2 of Fig. 1 ( $T_2 \approx 5$  K) similar calculations yield  $1/\tau_g^+ = 3 \cdot 10^6 \ s^{-1}$ .

4. We have not yet attempted in Refs. 1-3 and in the

present paper to specify concretely the course of  $D^{-}$  band electron capture by AC. We try this now. The capture can be regarded as a slow (owing to the very small mobility  $\mu_g$ ) slippage of electrons to AC under the action of the center's Coulomb field  $e/\kappa R^2$  (named "creeping recombination" by B. I. Shklovskiĭ<sup>11</sup>). The electron flux to an AC through the surface of a sphere of radius R is obviously equal to  $n_g\mu_g(e/\kappa R^2)4\pi R^2$ . Dividing this expression by  $n_g$  we obtain the capture coefficient

$$\alpha_{g}^{+} = 4\pi e \mu_{g} / \varkappa. \tag{7}$$

In the paper by Vorozhtsova *et al.*,<sup>3</sup> measurements at small *E* at  $T \simeq 3$  K yielded by an independent method, for an Si:B sample with  $N = 3 \cdot 10^{16}$  cm<sup>-3</sup> and  $K = 4 \cdot 10^{-5}$ ,  $\mu_g = 3 \text{ cm}^2/\text{V} \cdot \text{s}$  and  $\alpha_g^+ \simeq 5.8 \cdot 10^{-7} \text{ cm}^3 \cdot \text{s}^{-1}$ . Substitution of this value of  $\mu_g$  in (7) yields the very close value  $\alpha_g^+ = 4.8 \cdot 10^{-7} \text{ cm}^3 \cdot \text{s}^{-1}$ . So good an agreement is to some degree fortuitous, since the experimental  $\mu_g$  was quite approximate. On the other hand, from the values obtained above for  $\tau_g^+$  we obtain  $\alpha_g^+ \approx 8 \cdot 10^{-8} \text{ cm}^3 \cdot \text{s}^{-1}$  at  $E \simeq 60$  V/cm for sample 1 and  $8 \cdot 10^{-7} \text{ cm}^3 \cdot \text{s}^{-1}$  for sample 2 (E = 40 V/cm). In this case, too,  $\alpha_g^+$  can be regarded as in full accord with the creeping recombination. (It must be recognized that the field *E* should decrease  $\alpha_g^+$  somewhat.)

5. It was assumed above that the time  $\tau_g^+$  increases, and therefore  $\sigma_g$  rises somewhat at  $T < T_1$  with growth of T and E. For low T and small E, however, the growth of  $\sigma_g$  is very abrupt and attests to some qualitative change of the conducting properties of the  $D^-$  band in this sample at temperature somewhat below 3 K.

Let us set forth our understanding of the nature of the threshold of the conductivity  $\sigma_{g}$ . The electron is directed ("trickles" down) towards the nearest AC. This does not mean that the electron is necessarily captured by this center. The "trickling" process is hindered by diffusion. If the distance to the AC is not too short, and the diffusion is intense enough, the electron can go from the vicinity of the given AC to the vicinity of another, then reach the vicinity of a third, etc. In this case the electron covers in the crystal a distance  $\sim (D_{\sigma}\tau_{\sigma}^{+})^{1/2}$  much longer than the average distance  $R_c^+ \sim (N^+)^{-1/3}$  between the AC ( $D_g$  is the diffusion coefficient in the  $D^{-}$  band). Such an electron can be called "free": it contributes to the conductivity  $\sigma_g$ . If, however,  $(D_g \tau_g^+)^{1/2} < R_c^+$ , the electron should be regarded as captured and does not contribute to  $\sigma_g$ . An estimate of the critical temperature  $T_{cr}$  above which "free" electrons appear in the  $D^{-}$  band can be obtained from the relation

$$(D_g \tau_g^{+})^{\nu_h} \approx R_c^{+}. \tag{8}$$

Substituting here the equations

$$(\tau_{g}^{+})^{-1} = (4\pi e \mu_{g}/\varkappa) N^{+}, \quad \mu_{g} = e D_{g}/kT,$$

we obtain

$$e^2/\varkappa R_c^{-} \approx kT_{\rm cr}.\tag{9}$$

Note that the quantity on the left is the mean fluctuation of the potential produced by the randomly disposed AC. It can be regarded as the energy distance between the mobility edge and the percolation level in the  $D^{-}$  band. The experimental value of  $T_{\rm cr}$  of sample 1 in a field 40 V/cm is  $\simeq 2.8$  K (Fig. 1). From relation (9) we obtain  $T_{\rm cr} = 4$  K. Recognizing that our estimate is crude, the agreement should be regarded as good. For sample 2, calculation yields  $T_{\rm cr} \simeq 2$  K. The experimental value of  $T_k$  is somewhat lower (see curve 1' of Fig. 2).

It is customary in recombination theory to introduce a distance  $R_T = e^2/\kappa kT$  (see, e.g., Ref. 4). It can be regarded as the radius of a sphere surrounding the recombination center, in which the capture takes place. Condition (9) means that  $R_T \approx R_c^+$ , or

$$N^+ R_T^3 \approx 1. \tag{10}$$

At  $R_T \ge R_c^+$  the capture spheres cover fully the entire crystal. Since  $\sigma_g \simeq 0$  in this case, all the  $D^-$ -band electrons contained in the capture sphere should be regarded as captured. Assume this to be the case also at  $R_T < R_c^+$  (a free electron passing through this sphere has only a certain capture probability<sup>4</sup>). The crystal-volume capture in which the  $D^-$ -band electrons can be regarded as free is then

$$x_{T} = 1 - N^{+} R_{T}^{3}. \tag{11}$$

Expressing d in terms of T we get

$$x_T = 1 - (T_{\rm cr}/T)^3.$$
 (12)

At  $x_T \leq 1$  the  $\sigma_g(T)$  dependence should be determined by the function  $x_T(T)$ :  $\sigma_g(T) \propto x_T(T)$ . We have used dashed lines for the plots of  $x_T(T)$  in Fig. 1, in relative units, using a fit parameter  $T_{cr} = 2.77$  K (curve 5). In addition, the figure shows a plot of  $\sigma_g(T)/x_T(T)$  in a field 40 V/cm (curve 6). We see that the function  $x_T(T)$  agrees well with the form of curve 2' near  $T = T_{cr}$  and that the ratio  $\sigma_g(T)/x_T(T)$  varies smoothly with temperature in a manner close to the  $\sigma_g$  dependence at large values of  $E(\sigma_g(T) \propto T^2)$  (Ref. 3).

6. The Coulomb well becomes deformed in the presence of E. At a distance  $R > R_E$ , where  $e^2/\pi R_E^2 = eE$ , the influence of the field is stronger than that of the AC. The effect of the field on the recombination becomes substantial at  $R_E < \min(R_c^+, R_T)$ . The relative number of "free" electrons in the  $D^-$  band can be expressed, by analogy with (11), as

$$x_E(E) = 1 - N^+ R_E^3. \tag{13}$$

If  $R_T > R_c^+$ , a fast growth of  $\sigma_g(E)$  should be expected near the critical value  $E = E_{cr}$  is determined from the relation

$$N^+ R_E^{3}(E_{\rm cr}) \approx 1$$
. (14)

Curve 7 of Fig. 3b ( $T \approx 2.5$  K) applies to the case  $R_T > R_c^+$ and corresponds to  $E_{cr} \approx 26$  V/cm. An estimate using (14) yields the very close value  $E_{cr} = 30$  V/cm. Expressing  $N^+$ in terms of  $E_{cr}$  we obtain from (13)

$$x_{E}(E) = 1 - (E_{cr}/E)^{3/2}.$$
 (15)

For  $x_E \ll 1$  we have  $\sigma_g(E) \propto x_E(E)$ . Curve 8 of Fig. 3b shows the  $x_E(E)$  dependence for  $E_{cr} = 26$  V/cm, while curve 9 (dashed) shows the smooth part of the function  $\sigma_g(E)$ , [i.e., the ratio  $\sigma_g(E)/x_E(E)$ ] for T = 2.5 K. Everything stated above concerning the functions represented by curves 2', 5, and 6 of Fig. 1 can obviously be restated for the field dependences represented in Fig. 3b by curves 7, 8, and 9 respectively.

7. At  $T < T_1$  the conductivity  $\sigma_g \sim \mu_g \tau_g^+$  does not contain  $\mu_g$  and is inversely proportional to  $N^+$ . The relation  $\sigma_g \propto 1/N^+$  was actually observed in our measurements. Thus, for example, according to Figs. 1 and 2, at E = 60 V/cm and T = 3 K the value of  $\sigma_g$  for the second sample is approximately 6 times larger than for the first. The corresponding ratio of the densities  $N^+$  is  $0.15 = (6.7)^{-1}$ .

8. We conclude with a few remarks. The function  $x_T(T)$  [or  $x_E(E)$ ] is the fraction of the "free" electrons in the  $D^-$  band;  $\tau_g^+$  is the lifetime in the  $D^-$  band. The product  $x_T \tau_g^+$  [or  $x_E \tau_g^+$ ] can be regarded as the lifetime of the electrons of the  $D^-$  band in the conducting state. We note in this connection that the assumption that two lifetimes exist in the  $D^-$  band was set forth earlier in Ref. 3.

In the discussion of the form of  $\sigma_g(T)$  we have implicitly assumed that the  $D^{-}$ -band electrons are thermalized to a considerable degree. This assumption is corroborated by the strong dependence of  $\sigma_g$  on T for small E.

The analysis set forth is, of course, very crude and many premises call for substantial refinement. In particular, the introduction above of a  $T_{cr}$  independent of E (or  $E_{cr}$  independent of T) is apparently permissible only if  $R_E \gg R_T (T_{cr})$  [or respectively  $R_T \gg R_E (E_{cr})$ ]. In general,  $T_{\rm cr}$  should be a function of E, just as  $E_{\rm cr}$  a function of T. Further, in an electric field, the volume in which an electron is trapped is no longer spherical. Equation (13) should therefore read  $x_E(E) = 1 - \theta(E) N^+ R_E^3$ , where  $\theta(E)$  is a numerical factor of order unity.

The here-developed picture of  $D^{-}$ -band electron recombination on AC permits a qualitative description of the aggregate of the experimental result and, most importantly, account for the threshold-like onset of  $\sigma_g$  when T and E increase. The obtained  $T_{\rm cr}$  and  $E_{\rm cr}$  turn out to be close enough to the experimental values.

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<sup>1)</sup>The terminology belongs to B. I. Shklovskiĭ.

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