## Relaxation of the $\mu^+$ -meson spin in tellurium

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From measurements of the relaxation of the  $\mu^+$ -meson spin in strong magnetic fields it is concluded that a paramagnetic state ( $\mu^+e^-$ ) is formed in tellurium at temperatures 250–290 K.

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Relaxation of the  $\mu^*$ -meson spin in tellurium has been observed in a longitudinal magnetic field H and transverse magnetic field  $H_{\perp}$ . The work was carried out in the synchrotron at the Joint Institute for Nuclear Research, Dubna. The results are shown in Figs. 1-3. The relaxation rates shown in these figures  $\Lambda$  in a longitudinal magnetic field and  $\Lambda_{\perp}$  in a transverse field, and also the experimental asymmetry coefficients C of the angular distribution of positrons from  $\mu^* + e^*$  decay in a longitudinal magnetic field, were determined by the method of maximum likelihood with comparison of the experimental dependences N(t) of the number of positrons from  $\mu^* + e^*$  decay emitted opposite to the direction of the primary polarization of the  $\mu^*$  meson, and the corresponding theoretical expressions:

$$N(t) = N_0 e^{-t/\tau_0} (1 - C e^{-\Delta t})$$
(1)

for a longitudinal magnetic field and

$$N(t) = N_0 e^{-t/\tau_0} (1 - C e^{-\Delta t} \cos \omega t)$$
<sup>(2)</sup>

for a transverse magnetic field. Here  $\tau_0 = 2.2 \times 10^{-6}$  sec is the lifetime of the  $\mu^+$  meson;  $\omega$  is the Larmor precession frequency of the  $\mu^+$  meson in a field  $H_{\perp}$ . In the expressions (1) and (2) it is assumed that relaxation of the  $\mu^+$ -meson spin in tellurium occurs according to an exponential law:  $P(t)=e^{-\Lambda t}$ . The exponential dependence of P(t) in tellurium has been confirmed experimentally.

From the experimental dependence  $\Lambda(H)$  given in Fig. 1 for the relaxation rate as a function of the longitudinal magnetic field strength at T=290 K and T=250 K it follows that in tellurium at these temperatures a paramagnetic state ( $\mu^+e^-$ ) is formed. An experimental study of the ( $\mu^+e^-$ ) paramagnetic state by means of a longitudinal

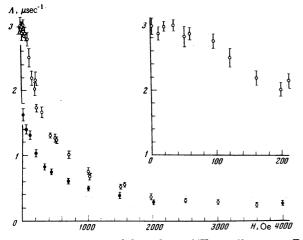


FIG. 1. Experimental dependence  $\Lambda(H)$  in tellurium at  $T = 290 \text{ K}(\bigcirc)$  and  $T = 250 \text{ K}(\bullet)$ . In the insert we have given the dependence  $\Lambda(H)$  at T = 290 K for H < 200 Oe.

magnetic field was first carried out for germanium.<sup>1</sup> A long-lived paramagnetic state  $(\mu^+e^-)$  in tellurium follows from the high relaxation rate  $\Lambda \sim 10^6$  sec<sup>-1</sup> of the  $\mu^+$ -meson spin, which is not suppressed even by a longitudinal field  $H \sim 10^3$  Oe. Such a large value of  $\Lambda$  can occur only in the interaction of the  $\mu^*$  meson with the electronic magnetic moment. The fact that  $\Lambda$  changes with change of magnetic field for  $H \approx 10^3$  Oe means that the observed relaxation of the  $\mu^+$ -meson spin cannot be the result of interaction with conduction electrons.<sup>1</sup> A natural explanation of the observed relaxation is the assumption of existence of an orbital bound state  $(\mu^+e^-)$  in this semiconductor. Precession of the  $\mu^*$ -meson spin in a transverse magnetic field  $H_{\perp}$  with frequency  $\omega$  is explained in this model by the high frequency  $\nu > \omega_0$  (Ref. 2) of flipping of the electron spin as the result of incoherent interactions with matter.

Let us now consider the process of  $\mu^+$ -meson spin relaxation in tellurium more in detail. It is evident from Fig. 2 that the coefficient *C* on increase of *H* first rises and then decreases. The rise of *C* can be explained if we assume that formation of the long-lived paramagnetic state ( $\mu^+e^-$ ) occurs as the result of interaction with matter of a short-lived experimentally unobserved atom of muonium. On increase of the longitudinal magnetic field *H* the depolarization of the  $\mu^+$  meson during the lifetime of the short-lived muonium atom decreases, which leads to an increase of the coefficient *C* in low fields  $H \leq 500$  Oe. The decrease of *C* in longitudinal fields H > 500 Oe can occur only as the result of a nonzero polarization of the  $\mu^+$ -meson spin as  $t \rightarrow \infty$ , i.e.,

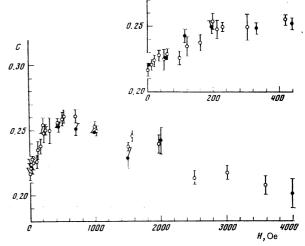
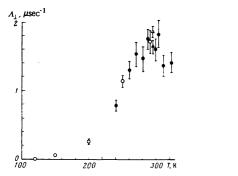
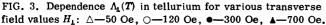


FIG. 2. Experimental dependences C(H) in tellurium at  $T = 290 \text{ K}(\bigcirc)$  and  $T = 250 \text{ K}(\bigcirc)$ . The dependence C(H) for T = 250 K for H < 400 Oe is given only in the upper figure.





as the result of stopping of the depolarization of the  $\mu^*$ meson spin after some time *t* following formation of the  $(\mu^*e^-)$  paramagnetic state, for example, on entry into a diamagnetic compound. Here the decrease of *C* should apparently be accompanied by a decrease of the relaxation rate  $\Lambda$ .

The existence of a short-lived muonium atom and the stopping of the  $\mu^*$ -meson depolarization according to a law  $e^{-t/\tau}$  lead to the following expression for the experimentally observable dependence N(t):

$$N(t) = N_0 e^{-t/\tau_0} [1 - a P_0(H) P(t)], \qquad (3)$$

where

 $P(t) = P_{\infty} + (1 - P_{\infty}) e^{-(\Lambda_1 + \Lambda_2)t} = \Lambda_1 \Lambda^{-1} [1 + \Lambda_2 \Lambda^{-1} e^{-(\Lambda_1 + \Lambda_2)t}]$ 

is the time dependence of the  $\mu^*$ -meson polarization. Here *a* is the experimental asymmetry coefficient of positrons from  $\mu^* \rightarrow e^*$  decay which has been observed at t = 0 in the absence of any unobserved  $\mu^*$ -meson depolarization processes; the value  $a = 0.278 \pm 0.005$  for tellurium was determined in a special experiment, where instead of tellurium a similar target of copper was installed;  $P_0(H)$  is the polarization of the  $\mu^*$  meson of the short-lived muonium atom remaining at the moment of formation of the long-lived ferromagnetic state;  $P_{\infty}$  is the polarization of the  $\mu^*$  meson as  $t \rightarrow \infty$ ;  $\Lambda_1 = \tau^{-1}$ is the probability of formation of a diamagnetic compound;  $\Lambda_2$  is the  $\mu^*$ -meson spin relaxation rate in the paramagnetic state ( $\mu^*e^-$ ), which depends on H;  $\Lambda = \Lambda_1$ + $\Lambda_2$  is the experimentally observed relation rate.

In Fig. 4 we have shown the dependence obtained from Eqs. (1) and (3) for T=290 K:

$$P_{\alpha}(H) = C \left( \frac{1}{\Lambda_{\alpha}\Lambda_{\alpha}^{-1}} \right) / a \left( C + \Lambda_{\alpha}\Lambda_{\alpha}^{-1} \right).$$

$$\tag{4}$$

The parameter  $\Lambda_1 = 0.080 \pm 0.005 \ \mu \text{ sec}^{-1}$  entering into this

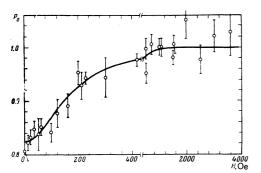


FIG. 4. Experimental (4) and theoretical (5) dependences  $P_0(H)$  in tellurium at T=290 K.

TABLE I. Parameters of expression (5) for  $P_0^{\text{theo}}$  (*H*) obtained by the method of maximum likelihood in comparison with the exceptional values (4).

<i>т</i> , к	т, µsec	ω'₀τ′	H <sub>0</sub> ', Oe	τ' X 10 <sup>10</sup> , sec	X <sup>2</sup>	n –
<b>29</b> 0	12.5±0.8	$0.74 \pm 0.02$	101±8	4.2±0.4	17	25
<b>25</b> 0	12.5±1.6	$0.75 \pm 0.05$	76±11	5.6±1.2	9	11

expression was chosen in such a way that the values of  $P_0$  determined by Eq. (4) increase monotonically within the statistical errors with increase of the field *H* and satisfy the condition  $P_0 < 1$ . The experimental dependence  $P_9(H)$  in Fig. 4 is compared with the theoretical expression<sup>2</sup>

$$P_{0}^{\text{theo}}(H) = \frac{1 + (\omega_{0}'\tau')^{2}(1/2 + x^{2})}{1 + (\omega_{0}'\tau')^{2}(1 + x^{2})}$$
(5)

for the residual polarization of the short-lived muonium in a longitudinal field  $x=H/H'_0$  for  $\nu=0$ . Here  $\omega'=2\beta H'_0/\pi$ and  $\tau'$  are the hyperfine-splitting frequency and the lifetime of the muonium atom;  $\beta$  is the magnetic moment of the electron.

It is evident from Fig. 4 that the theoretical expression (5) satisfactorily describes the experimental dependence (4)  $P_0(H)$  for T=290 K. The same good agreement is observed also for T=250 K with  $\Lambda_1=0.080\pm0.010$   $\mu$  sec<sup>-1</sup>. The corresponding values of the parameters  $\omega_0'\tau'$ ,  $H'_0$ , and  $\tau'$ , and also the values of the Pearson parameter  $\chi^2$ , are given in the Table. We have also given in the Table the values  $\tau = \Lambda_1^{-1}$  of the mean life of the long-lived paramagnetic state ( $\mu^+e^-$ ) determined from Eq. (4); n is the number of experimental values of  $P_0(H)$ .

It must be emphasized that the use of Eq. (5) for  $P_0^{\text{theo}}(H)$  does not assume the equality  $\nu = 0$ . Use of this formula means only that the relation  $\nu < (\tau')^{-1} = 0.24 \times 10^{10}$  sec<sup>-1</sup> (T = 290 K) is satisfied, which is consistent with the rather high frequency  $\nu > \omega_{0}$ .

In addition it should be noted that the mechanism of depolarization of the long-lived paramagnetic state  $(\mu^*e^-)$  remains unclear. The experimental dependence  $\Lambda(H)$ , which is not described by the expression

$$\Lambda_{2} = \nu / [4(\nu \omega_{0}^{-1})^{2} + x^{2}], \quad \nu > \omega_{0}, \tag{0}$$

obtained for the case in which the  $\mu^*$  meson is depolarized in interaction with a single paramagnetic electron,<sup>2</sup> needs explanation. Also requiring explanation is the dependence shown in Fig. 3 of  $\Lambda_{\perp}(T)$  in a transverse magnetic field  $H_{\perp}$ . It is evident from Fig. 3 that the value of  $\Lambda_{\perp}$  increases with increasing temperature, remaining 1.5-2 times less than the values  $\Lambda(H=0)$ .

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