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RESONANCE SCATTERING OF GAMMA QUANTA BY Mg²⁴ NUCLEI

D. K. KAIPOV, Yu. K. SHUBNYĬ, V. M. AMERBAEV, A. KAZANGAPOV, and Yu. G. KOSYAK

Nuclear Physics Institute, Academy of Sciences, Kazakh SSR

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Resonance scattering of 1.38-MeV γ quanta by Mg²⁴ nuclei was investigated using a source of radioactive Na²⁴ in the form of an aqueous solution of NaOH. The average cross section for resonance scattering was found to be $(3.7 \pm 0.6) \times 10^{-28}$ cm². The energy distribution of the emitted γ quanta was calculated for the $\beta - \gamma_2 - \gamma_1$ cascade taking account of the slowing down of the recoil nuclei. The lifetime of the 1.38-MeV level in Mg²⁴ was determined to be $(1.1 \pm 0.2) \times 10^{-12}$ sec.

 $\begin{array}{l} R_{\text{ECENT}} \text{ investigations}^{[1-3]} \text{ have shown that resonance scattering of } \gamma \text{ quanta by nuclei can occur} \\ \text{when one uses liquid and solid sources, provided} \\ \text{the lifetime } \tau_{\gamma} \text{ of the initial level is less than} \\ 10^{-12} \text{ sec. Since the time between collisions of the} \\ \text{recoil nuclei with surrounding atoms is of order} \\ 10^{-13} - 10^{-14} \text{ sec, the slowing down of the recoil nuclei results in a change in the energy distribution} \\ P(E) \text{ of the } \gamma \text{ quanta.} \end{array}$

To determine τ_{γ} one must find experimentally the average cross section for resonance scattering and calculate the microspectrum P(E) theoretically. A calculation of the microspectrum, with account of the slowing down of the recoil nuclei, is necessary mainly for two reasons. First, in certain cases, in particular when using very shortlived isotopes, obtaining a source in the gaseous state or the use of the "self-absorption" method for determining τ_{γ} is a difficult experimental problem. Second, the study of the attenuation of the resonance effect in dense media can give information about the lifetimes of higher-lying levels. In our work we studied the resonance scattering of 1.38-MeV γ quanta by Mg²⁴ nuclei, using the radioactive isotope Na²⁴ (T_{1/2} = 14 hr) in the form of an aqueous solution of NaOH. The Na²⁴ decay is accompanied by the emission of a β particle with endpoint $E_{max} = 1.39$ MeV and two γ quanta with energies $E_{\gamma_2} = 2.76$ MeV and $E_{\gamma_1} = 1.38$ MeV.

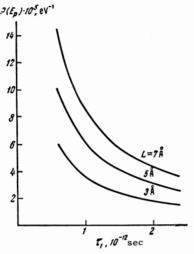
To compute the spectrum P(E), we used a model with continuous slowing down of the recoil nuclei as the result of elastic collisions with the surrounding atoms. The energy of the emitted γ_1 quantum was

$$E_{\gamma i} = (E_{\gamma i}^{0} / Mc) p_{2x} + [E_{\gamma i}^{0} - (E_{\gamma i}^{0})^{2} / 2Mc^{2}] = ap_{2x} + b,$$

where $E_{\gamma_1}^0$ is the energy of the level, p_{2x} is the projection of the total momentum on the direction of emergence of the γ_1 quantum, and the energy distribution of the γ quanta is given by the density distribution of the momentum projection ξ (p_{2x}^{ν}):

$$P(E) = \xi(p_{2x}) / a.$$
 (1)

For the case of a $\beta - \gamma_2 - \gamma_1$ cascade, the density distribution of recoil nuclei over momentum pro-



Dependence of $P(E_p)$ on r_1 , computed theoretically for various values of the free path L.

jections, taking account of the slowing down, was found to be

$$\xi(p_{2x}'') = \frac{M^{5}L^{5}}{4p_{\gamma_{2}}\tau_{1}\tau_{2}} \int_{|p_{2x}''|}^{p_{max}+p_{\gamma_{2}}} dp_{2x}'' \int_{\lambda_{2}}^{\lambda_{1}} \frac{\exp(-t_{1}/\tau_{1}) dt_{1}}{(ML - p_{2}''t)^{3}} \\ \times \int_{\left|\frac{MLp_{2}''}{ML - p_{2}''t_{1}} - p_{\gamma_{2}}\right|}^{p_{max}} \frac{dp'}{p'} \int_{0}^{\lambda_{0}} \exp\left(-\frac{t}{\tau_{2}}\right) g\left(\frac{MLp'}{ML - p't}\right) \\ \times \frac{dt}{(ML - p't)^{2}}, \\ \lambda_{0} = ML\left(\frac{1}{p'} - \frac{1}{p_{max}}\right), \quad \lambda_{1} = ML\left(\frac{1}{p''} - \frac{1}{p_{\gamma 2} + p_{max}}\right), \\ \lambda_{2} = ML\left(\frac{1}{p''} - \frac{1}{p_{\gamma 2} - p_{max}}\right) \eta(p_{\gamma 2} - p_{max} - p_{2}'').$$
(2)

Here g(p) is the momentum distribution of the recoil nuclei, p_{max} is the maximum momentum after the β decay, p_2'' is the total momentum after the β and γ_2 transitions, $p\gamma_2$ is the momentum of the recoil nucleus from the γ_2 transition, τ_1 and τ_2 are the lifetimes of the first and second excited states, and L is the mean free path.

Theoretical values of ξ ($p_{2x}^{\prime\prime}$) were computed on the "Minsk" computer for the cases of the Na²⁴ \rightarrow Mg²⁴ and Co⁶⁰ \rightarrow Ni⁶⁰ decays, with different values of τ_1 , τ_2 , and L. The computations showed that for Co⁶⁰ \rightarrow Ni⁶⁰ the value of P(E_p) depends on τ_2 , which is easily understood considering that $E_{\gamma_2} < E_{\gamma_1}$. For Na²⁴ \rightarrow Mg²⁴ ($E_{\gamma_2} > E_{\gamma_1}$), the value of P(E_p) depends only on τ_1 and L and is independent of τ_2 , which is explained by the position of the resonance line in the microspectrum.

The figure shows the dependence found for $P(E_p)$ on τ_1 for different values of L. Consequently, assigning L, we can determine τ_1 if we know the average cross section $\overline{\sigma}$ for resonance scattering of 1.38-MeV γ quanta by Mg²⁴ nuclei. The determination of $\overline{\sigma}$ was done in an apparatus similar to one used earlier.^[4] The initial Na^{24} activity was 0.5 Ci. Since the resonance effect also occurs in solid Na²⁴, ^[1,5] to measure the scattering from scatterers of magnesium and aluminium under nonresonant conditions we used the radioactive isotope La^{140} (T_{1/2} = 40 hr) with transition energy 1.59 MeV. The determination of the average cross section for resonance scattering was done by numerical integration over the scatterer surface. We found the value $\overline{\sigma}$ = $(3.7 \pm 0.6) \times 10^{-28} \text{ cm}^2$.

Analysis of the data found from resonance scattering of γ quanta emitted after a β transition^[4,3] shows that the mean free path of the recoil nuclei in water solution is (1.5 ± 0.3) $\times 10^{-8}$ cm, which gives L = $(5.0 \pm 1.0) \times 10^{-8}$ cm for the case considered. Using the experimental value of $\overline{\sigma}$ and the theoretical dependence of P(E_p) on τ_1 , we find

$$\tau_1 = (1.1 \pm 0.2) \cdot 10^{-12}$$
 sec.

The result is in satisfactory agreement with the data of other work on resonance scattering of 1.38-MeV γ quanta by Mg²⁴ nuclei.

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