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## ALPHA DECAYOF Pu<sup>241</sup>

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The  $\alpha$  spectrum of Pu<sup>241</sup> was studied with a magnetic  $\pi\sqrt{2}$   $\alpha$  spectrometer. The following  $\alpha$  transitions were observed (in keV): 5042 (1.5%), 4973 (1.4%), 4899 (83%), 4862 (13%), and 4805 (1.1%). The decay scheme of Pu<sup>241</sup> is discussed.

THE investigation of the  $\alpha$  decay of Pu<sup>241</sup> (T = 13 years)<sup>[1]</sup> is very complicated because: 1) Only 2.3 × 10<sup>-3</sup>% of the decays are  $\alpha$  de-

cays, <sup>[2]</sup> corresponding to an  $\alpha$  half-life of 5.7  $\times 10^5$  years.

2) The intensity of all  $Pu^{241} \alpha$  transitions in the investigated samples was, as a rule, hundreds of times smaller than the  $\alpha$ -transition intensities of  $Pu^{238}$  and  $Pu^{240}$  at higher energies  $E_{\alpha}$ . This means that the  $Pu^{241}$  lines are located in the tails of the  $Pu^{238}$  and  $Pu^{240}$  lines.

3) The energies of the main  $Pu^{241} \alpha$  transitions are very close to the energies of  $Pu^{242} \alpha$  transitions (Table I). It follows that the possibility of studying the  $Pu^{241} \alpha$  spectrum also depends on the  $\alpha$ -activity ratio of  $Pu^{241}$  and  $Pu^{242}$  in a given sample.

The foregoing circumstances appear to account for the fact that very little information regarding Pu<sup>241</sup>  $\alpha$  decay is found in the literature. Strominger, Hollander, and Seaborg<sup>[3]</sup> give data for two  $\alpha$  groups at 4893 and 4848 keV with 75% and 25% intensities, respectively. On the basis of data in <sup>[4]</sup> indicating the existence of a 145-keV  $\gamma$  line in the Pu<sup>241</sup>  $\gamma$  spectrum it was suggested in <sup>[3]</sup> that this  $\gamma$  line represents a transition from the 145-keV level of U<sup>237</sup>, reached by a 4893-keV  $\alpha$  transition, to the ground state. The intensity of this transition is the fraction  $2 \times 10^{-6}$  of Pu<sup>241</sup> decays; this corresponds to  $2 \times 10^{-6}/2.3 \times 10^{-5}$ = 9% of the number of  $\alpha$  decays. The  $\gamma$  spectrum also reveals a line at about 100 keV, which appears to be a K x-ray line of U<sup>237</sup> with the intensity  $1 \times 10^{-5}$ , i.e.,  $1 \times 10^{-5}/2.3 \times 10^{-5} = 45\%$ of the number of  $\alpha$  decays.

Information regarding the  $U^{237}$  level scheme can also be obtained by studying the  $\beta$  decay of  $Pa^{237}$ . The first data regarding the  $\beta$  decay of this isotope, to which the half-life 11 min was assigned, appeared in <sup>[5]</sup>. Subsequently  $39 \pm 3$  min was obtained for the half-life by Takahashi and Morinaga,<sup>[6]</sup> who observed three endpoints at 2.30, 1.35, and 0.8 MeV in the  $\beta$  spectrum of  $Pa^{237}$ , as well as 17  $\gamma$ lines from 90 to 1420 keV. These included the aforementioned 145-keV transition. One possible  $Pa^{237}$  decay scheme, based on these data, was discussed.

#### EXPERIMENT

We studied the Pu<sup>241</sup>  $\alpha$  spectrum using the magnetic  $\pi\sqrt{2}$   $\alpha$  spectrometer of the Radium Institute of the Academy of Sciences.<sup>[7]</sup> The measurements were obtained under the same conditions as in our



FIG. 1. Portion of  $Pu^{241} \alpha$  spectrum.  $E_{\alpha} - \alpha$ -particle energy,  $N_{\alpha} -$  number of  $\alpha$  tracks in a band  $300\mu$  wide.

investigation of the  $\alpha$  spectra of curium isotopes.<sup>[8]</sup> The 1 × 10-mm source was prepared by vacuum deposition on glass. The surface density of about 20  $\mu$ g/cm<sup>2</sup> resulted in a broadening of the  $\alpha$  lines (10-11-keV half-width) and some lengthening of their tails. This source thickness was required in order to obtain information about the relatively weak Pu<sup>241</sup> lines.

Each of the four exposures lasted 90 hours. Figure 1 shows a portion of the  $\alpha$  spectrum of plutonium isotopes in the energy range 4.75-5.10 MeV, obtained in one of the exposures. The spectrum was recorded when 5.05-MeV  $\alpha$  particles moved in a circular orbit. During the other exposures the magnetic fields were somewhat differerent, and the  $\alpha$  particles moved in circular orbits at the energies 5.15, 4.95, and 4.88 MeV. Table I gives our results together with some previously tabulated data. The  $\alpha$  spectra of the isotopes Pu<sup>238,240,242</sup> have been studied very thoroughly, so that any observed  $\alpha$  line not be-longing to any one of these isotopes can be assigned to Pu<sup>241</sup>. In each instance the  $\alpha$  energies were also compared with data for all possible  $\alpha$ -active impurities. The table gives the  $\alpha$ -transition energies. The reference line is Pu<sup>240</sup>  $\alpha_2$  at 5020 keV (line No. 2), whose energy is known very accurately ( $\pm 2 \text{ keV}$ ).<sup>[3,9]</sup>

There is a notable disagreement with the values that we obtained in earlier work for the  $Pu^{242} \alpha$ transitions and the most intense  $Pu^{241}$  transition. The discrepancy of about 6 keV can be attributed to a shift of the energy scale toward higher values. This shift has recently been observed in the entire

Table	Ι
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No. of line	Plutonium	Tabulated data <sup>[3,9]</sup>		Our data	
	isotope to which the $\alpha$ transition is assigned	$E_{\alpha}$ , keV	Relative in- tensity in the isotope, %	$E_{\alpha}$ , keV	Relative in- tensity in the isotope, %
1 2 3 4 5 6 7 8	Pu <sup>241</sup> Pu <sup>240</sup> Pu <sup>241</sup> Pu <sup>241</sup> Pu <sup>241</sup> Pu <sup>241</sup> Pu <sup>242</sup> Pu <sup>241</sup>	5020 4898 4893 4848 4853	0,1 76 75 25 24	$5042 \pm 4 \\ 5020 \\ 4973 \pm 4 \\ 4904 \pm 3 \\ 4899 \pm 4 \\ 4862 \pm 4 \\ 4859 \pm 3 \\ 4805 \pm 4$	$1.5\pm0.50.11.4\pm0.375\pm283\pm813\pm325\pm21.1\pm0.3$

range of  $\alpha$  energies. Our reference line in these measurements was the 5020-keV Pu<sup>240</sup> line; this value corresponds to the energy of the 5169-keV  $Pu^{240}$  main transition given in [9]. In earlier work the assigned energies of the Pu<sup>240</sup>  $\alpha_0$  and  $\alpha_2$ groups were 5162 keV and 5014 keV, respectively.<sup>[3]</sup> This can possibly account for the too low energies of the main  $Pu^{242}$  and  $Pu^{241}$  transitions given in <sup>[3]</sup>.

The experimental curve (Fig. 1) reveals, in addition to the single lines Nos. 1, 3, and 8, two composite lines 4-5 and 6-7, whose half-widths show that they are at least double lines. From earlier work it is known that these lines should include doublets of the main  $Pu^{241}$  and  $Pu^{242}$  lines. We were unable to resolve these lines experimentally because of low resolving power. The resolution shown in Fig. 2 is based on the following considerations.



FIG. 2. Resolution of lines 4-5 and 6-7 (Pu<sup>241</sup> and Pu<sup>242</sup>) (on photographic plate).

First, the line shape in this region was determined from the line  $\alpha_2$  Pu<sup>240</sup> (line No. 2). However, a resolution based only on knowledge of the line shape could result in a large error (greater than 20%) in both the intensities and energies of the transitions.

Secondly, lines 4 and 7 belong to the  $Pu^{242} \alpha$ spectrum, representing transitions to the  $0^+$  and  $2^+$  levels of  $U^{238}$ . According to the literature these lines differ by 45 keV (from  $\alpha$  spectra<sup>[3]</sup> and Coulomb excitation<sup>[10]</sup>) and their intensity ratio is 76/24.<sup>[3]</sup> Also, the intensity ratio of  $\alpha$  transitions to the  $0^+$  and  $2^+$  levels of all neighboring even-even nuclei does not vary much; the average ratio is  $(75 \pm 2)/(25 \pm 2)$ . Lines 4–7 can therefore be resolved quite accurately  $(\pm 10\%)$ , because, in addition to the line shape, we know the energy difference of lines 4 and 7, and their intensity ratio.

As a result of the foregoing line resolution it was found that

1) the energy difference of  $Pu^{242}$  line No. 4 and Pu<sup>241</sup> line No. 5 agrees with the literature; 2) the energy of Pu<sup>241</sup>  $\alpha$  transition No. 6 is

higher than the energy of  $Pu^{242}$  transition No. 7, thus conflicting with the results of Asaro et al.;<sup>[3]</sup>

3) the intensity ratio of  $Pu^{241}$  lines 5 and 6 is  $(83 \pm 8)/(13 \pm 3)$ , which also disagrees with the results of Asaro et al., <sup>[3]</sup> who obtained 75/25.

At energies below 4.8 MeV we observed no Pu<sup>241</sup>  $\alpha$ -decay lines with intensities above 0.2%.

Table I shows our data for the relative intensities of  $\alpha$  transitions in each plutonium isotope. Table II gives the excitation energies of U<sup>237</sup> levels and the hindrance factors F for the  $\alpha$  transitions, calculated from the data of Bohr et al.<sup>[11]</sup>

## DISCUSSION OF Pu<sup>241</sup> DECAY SCHEME

The Pu<sup>241</sup> ground-state spin was found by means of magnetic resonance to be  $\frac{5}{2}$ . [12] This agrees well with the Nilsson scheme for single-particle states of deformed nuclei. The ground state of a nucleus containing 147 neutrons is a  $\frac{5}{2}$  [622] level.

### A. Transitions with small F

The hindrance factor for the 4899-keV  $\alpha$  transition is 1.5, which indicates that the transition is favored and goes to a  $\frac{5}{2}^+$  state. The 4862- and 4805-keV transitions are also characterized by small values of F (5.2 and 25.0); this is characteristic of transitions to levels of a single rotational band, which in the present case has the quantum number  $K = \frac{5}{2}$ . The probability ratios of  $\alpha$  transitions to rotational band levels as calculated from the formula in [11] for  $Pu^{241}$  are

$$J(5/_2 \rightarrow 5/_2): J(5/_2 \rightarrow 7/_2): J(5/_2 \rightarrow 9/_2) = 100: 13: 2.2.$$

This result agrees satisfactorily with our ratio 100:16:1.3, thus confirming the hypothesis that the three U<sup>237</sup> levels reached by favored decays are members of the  $K = \frac{5}{2}$  rotational band which have spins and parities  $\frac{5}{2}^{+}$ ,  $\frac{7}{2}^{+}$ , and  $\frac{9}{2}^{+}$ . The transition intensity ratio  $J(\frac{5}{2} \rightarrow \frac{5}{2}): J(\frac{5}{2} \rightarrow \frac{7}{2}) = 100:33$ given in <sup>[3]</sup> is evidently incorrect. However, the energy differences between these three levels are not in accord with the interval ratio derived from the formula for excited levels of the  $K = \frac{5}{2}$  rota-

Table II

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$a_{transition}^{\alpha}$	Eα, keV	Energy level,* keV	Relative intensity, %	Hindrance factor, F		
$\begin{array}{c} \alpha_0 \\ \alpha_1 \\ \alpha_2 \\ \alpha_3 \\ \alpha_4 \end{array}$	$5042 \pm 4$ $4973 \pm 4$ $4899 \pm 4$ $4862 \pm 4$ $4805 \pm 4$	$\begin{array}{c} 0 \\ 70 \pm 2 \\ 145 \pm 2 \\ 183 \pm 3 \\ 241 \pm 3 \end{array}$	$1,5\pm 0,5 \\ 1.4\pm 0,3 \\ 83\pm 8 \\ 13\pm 3 \\ 1.1\pm 0,3$	$700 \\ 250 \\ 1.5 \\ 5.2 \\ 25$		

\*Assuming that  $\alpha_0$  is a ground-state transition of U<sup>237</sup>.



tional band. Indeed,  $E_{rot}(\frac{9}{2}^{+}) = 96 \text{ keV}$  and  $E_{rot}(\frac{7}{2}^{+}) = 38 \text{ keV}$ , giving the ratio 2.53 instead of the computed ratio 16/7 = 2.29. The moments of inertia based on these levels are  $A = \frac{\hbar^2}{2I}$  = 5.42 keV from the  $\frac{7}{2}^{+}$  level and 6.00 keV from the  $\frac{9}{2}^{+}$  level.

It is extremely likely that the foregoing energy levels can be accounted for by the interaction between the nuclear rotational motion and the motion of the odd nucleon. Kerman<sup>[13]</sup> has considered the interaction of levels belonging to different rotational bands of identical parity but with K differing by unity. He showed that this interaction can make the energy levels in rotational bands differ from the calculated values. In the case of  $U^{237}$ we consider the interaction of the levels  $\frac{7}{2}$  $(K = \frac{5}{2} [622])$  and  $\frac{7}{2} + [624]$ , which causes a relative shift between them. The  $\frac{7}{2}$  [624] state is one of the closest to [622] in the Nilsson scheme. We did not observe this level experimentally, although it appears among the excited states of Pu<sup>239</sup>, which resembles U<sup>237</sup>, having an equal number of neutrons (N = 145).

## B. Relation between the transitions $\alpha_2$ and $\alpha_0$

The rotational band mentioned in paragraph A is clearly not a ground state band, because the transitions  $\alpha_0$  and  $\alpha_1$  occur at higher energies than  $\alpha_2$ . The  $\alpha_2$  transition is very intense (83% of the  $\alpha$  decays) and goes to a level which should be deexcited through intense  $\gamma$  radiation. The only known  $\gamma$  line of Pu<sup>241</sup> is  $h\nu = 145$  keV. This  $\gamma$ line probably follows the  $\alpha_2$  group immediately; this would mean that there is a level lying 145 keV below the rotational band, and the decay energy of group  $\alpha_0$  actually is 145 keV above that of group  $\alpha_2$ . Thus the groups  $\alpha_2$  and  $\alpha_0$  are consistent with the 145-keV  $\gamma$  rays with regard to energy.

FIG. 3. a and b – two different  $Pu^{241} \alpha$ -decay schemes; c –  $Cm^{243} \alpha$ -decay scheme.

#### C. Decay to the ground state of $U^{237}$

It is not clear from the foregoing whether the  $\alpha_0$  group represents decay to the ground state or to some low-lying state of  $U^{237}$ . In the latter case intense  $\gamma$  rays and conversion transitions should occur, but at a low transition energy they could remain unobserved in scintillation measurements. The fact that this level can have only a low excitation energy follows from consideration of a closed decay cycle. The pertinent cycle (of a 4n+1 nucleus) is

$$\begin{array}{c} Np^{237} \xleftarrow{} \begin{array}{c} Q_{\alpha} = 5.64 \text{ MeV} \\ \hline \end{array} & Am^{241} \\ 0.52 \text{ MeV} & \uparrow \beta \\ \hline \end{array} & \beta \uparrow 0.02 \text{ MeV} \\ \hline \\ U^{237} \xleftarrow{} \begin{array}{c} \alpha \\ Q_{\alpha} = ? \end{array} & Pu^{241} \end{array}$$

which gives 5.14 MeV as the total decay energy of  $Pu^{241}$ , with  $E_{\alpha_0} = 5.05$  MeV. This is very close to the  $\alpha_0$  transition energy (5042 keV), and it can therefore be assumed that this transition goes either to the ground state or to a close-lying state of  $U^{237}$ .

## D. Ground state of $U^{237}$

From a rigorous point of view nothing is known about the ground state of  $U^{237}$ . The Nilsson scheme predicts the state  $\frac{1}{2}$  [631] for the 145-th neutron. In the case of Pu<sup>239</sup>, which also has 145 neutrons, \* this prediction is confirmed; the experimental ground-state spin is  $\frac{1}{2}$  and the ground-state rotational band appears to have the quantum number  $K = \frac{1}{2}$ .<sup>[8]</sup> Figure 3c shows the lower portion of

the  $\operatorname{Cm}^{243} \xrightarrow{\alpha} \operatorname{Pu}^{239}$  decay scheme. The analogously constructed rotational band for  $U^{237}$  can appear either as in Fig. 3a (given by Takahashi and Mor-inaga<sup>[6]</sup>) or as in Fig. 3b. It should be noted that

the hindrance factor for  $\alpha_0$  (F = 700) does not conflict with either of these two versions of the decay scheme.

The Pu<sup>241</sup>  $\alpha$  spectrum contains the still unconsidered 4973-keV transition  $\alpha_1$  (70 keV less decay energy than for  $\alpha_0$ ). It is reasonable to assume that, as in the decay  $\text{Cm}^{243} \rightarrow \text{Pu}^{239}$ , this transition goes to one of the ground-state rotational levels. The essential difference between the decay schemes of Fig. 3, a and b, lies in the fact that in the former  $\alpha_1$  goes to the  $\frac{5}{2}$  level, while in the latter it goes to the  $\frac{7}{2}$  level.

The following arguments can be advanced against Fig. 3a:

1. There is a great difference between the moment of inertia (A = 7.7 keV) of the ground-state rotational band with K =  $\frac{1}{2}$  and that of the K =  $\frac{5}{2}$ band (A = 6.0 keV). We recall that in the case of Pu<sup>239</sup>, which resembles U<sup>237</sup>, the moments of inertia for these two bands are practically equal (6.25 and 6.30 keV, respectively) although the  $\frac{5}{2}^{+}$ energy level lies considerably higher (286 keV) in Pu<sup>239</sup> than in U<sup>237</sup> (145 keV).

2. The 145-keV  $\gamma$  transition occurs between  $\frac{5}{2}^{+}$  and  $\frac{1}{2}^{+}$  states and is thus of multipolarity E2. However, the total conversion coefficient for the 145-keV E2 transition is ~1.7, and the total intensity of the 145-keV transition is 24% of the number of  $\alpha$  decays. This number is considerably smaller than the population of the 145-keV level.

3. Our measurements reveal no  $\alpha$  transition to the 95-keV level. This means that if the transition does occur its intensity is at least one order smaller than that of the  $\alpha$  transition to the 70-keV level. On the other hand, it follows from the data on Cm<sup>243</sup>  $\frac{\alpha}{2}$ , Pu<sup>239</sup>  $\alpha$  decay that decay to the  $\frac{7}{2}$ <sup>+</sup> level is more intense than to the  $\frac{5}{2}$ <sup>+</sup> level, and that decay to the  $\frac{3}{2}$ <sup>+</sup> level is more intense than to the  $\frac{1}{2}$ <sup>+</sup> level.

For the decay scheme of Fig. 3b the first objection can be removed by a suitable selection of the decoupling factor a; for a = -0.166 and  $E(\frac{7}{2}^{*}) - E(\frac{3}{2}^{*}) = 70$  keV the moment of inertia is A = 6.0 keV as for the  $K = \frac{5}{2}$  band. The second objection is removed because the 145-keV transition can be mainly M1. Then  $\Sigma \alpha = 6.4$  and

the total transition intensity can be as high as 67%. In  $\text{Cm}^{243} \xrightarrow{\alpha} \text{Pu}^{239}$  this M1 transition is the main transition from the  $\frac{5}{2}$  (K =  $\frac{5}{2}$ ) level. The third objection disappears automatically.

It seems to us, however, that the aforementioned value a = -0.166 is not the most probable one. With this value of a,  $x = E(\frac{3}{2}) - E(\frac{1}{2})$ would have the value 15 keV, thus disagreeing with the energy balance in the foregoing cycle. By setting a = -0.620 we obtain A = 6.5 keV and  $x = E(\frac{3}{2}^{*}) - E(\frac{1}{2}^{*}) = 7$  keV; for Pu<sup>239</sup> we have A = 6.25 keV and x = 8 keV.

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