$$\sum_{\mathbf{x}, M} (-)^{M-K} C_{I-MIM}^{\mathbf{x}0} C_{I-KIK}^{\mathbf{x}0} D_{00}^{\mathbf{x}} (\omega) = 1, \qquad (8)$$

hence,

$$\sigma_{s}^{IK}(\theta) = \frac{2}{\pi} \frac{(kb)^{4}}{k^{2}} \int_{0}^{1} d\mu \xi^{2}(\mu) \int_{0}^{\frac{\pi}{2}} d\varphi \left[\frac{J_{1}(t)}{t}\right]^{2} = \sigma_{s}(\theta). \quad (9)$$

Thus, the differential scattering cross section  $\sigma_s(\theta)$  does not depend on the initial state of the nucleus, i.e., on the index *I*, *K*. Graphs of the function  $\sigma_s(\theta)$  for different degrees of nuclear deformation and different neutron energies have been published<sup>1</sup>.

The integrated cross section  $\sigma_s = \int d\Omega \sigma_s(\theta)$ , does not depend on the energy (in agreement with the results of Ref. 1) and has the form

$$\sigma_{s}=\pi b^{2}\int_{0}^{1}d\mu\xi\left( \mu\right) .$$

The dependence of  $\sigma_s$  on the degree of nuclear deformation was considered in Ref. 1.

The total cross section for all scattering processes is specified by the imaginary part of the amplitude for elastic scattering evaluated at  $\theta=0$ , i.e.,

$$\sigma_t^{IK} = \frac{4\pi}{K} \frac{1}{2I+1} \sum_M \operatorname{Im} f_{IMK}^{IMK}(\Omega) \left| \theta = 0 \right|^{-1}$$

This reduces with the use of Eq. (5) to the total cross section  $\sigma_t^{IK} = \sigma_t = 2\pi b^2 \int d\mu \xi(\mu) = 2\sigma_s$ . The cross section for capture is  $\sigma_c^0 = \sigma_t = \sigma_s = \sigma_s$ .

Thus, the total neutron scattering cross section and absorption cross section do not depend on the initial state of the nucleus either.

It is easy to see that for the case of spherical nuclei the above formulas reduce to the formulas given by the diffraction of neutrons' by "black" spherical nuclei.

The author expresses his gratitude to B. T. Geilikman and V. M. Strutinski for many valuable discussions. <sup>2</sup> A. Bohr and B. Mottelson, K. Danske. Vidensk Selsk. Mat.-fys. Medd., 27, No. 16 (1953).

Translated by A. Skumanich 157

## Concerning the Radiative Correction to the µ-Meson Magnetic Moment

V. B. BERESTETSKII, O. N. KROKHIN

AND

A. K. Khlebnikov

(Submitted to JETP editor January 7, 1956) J. Exptl. Theoret. Phys. (U.S.S.R.) 30, 788-789

(April, 1956)

NALYSIS of the structure of the present A quantum theory of fields indicates its inapplicability to distances of the order of  $\hbar / \lambda_0 \sim 10^{-13}$ -10<sup>-14</sup> cm<sup>1</sup>. Consequently, for those quantumelectrodynamic processes where momenta (real or virtual) of the order of  $\lambda_0$  play a role, deviations from the usual formulas are to be expected. For the evaluation of these deviations in the integrals which appear in the determination of radiative corrections (integrals over virtual momenta) one can restrict the upper limit of integration to  $\lambda_0$ . Since these integrals converge for momenta  $\sim m$ , then the deviations should be of the order of  $m^2/\lambda_0^2$ , where *m* is the mass of the charged particle. This is why the deviations for the magnetic moment of the electron appear only in the third order radiative correction, viz.,  $\alpha^3(\alpha = e^2/\pi c)^2$ . In the case of the heavier  $\mu$ -meson, the finiteness of  $\lambda_0$  affects the first radiation correction ( $\sim \alpha$ ) and one expects a different value than predicted by Schwinger's formula. If one assumes that the  $\mu$ -meson is devoid of any specific interactions which are greater than the electromagnetic one, then the problem can be treated as one in pure electrodynamics.

For the determination of the magnitude of the change in the radiative correction to the magnetic moment of the  $\mu$ -meson (a change which is dependent upon the finiteness of  $\lambda_0$ ) we shall consider, as is customary<sup>3,4</sup>, the vertex portion of the scattering matrix of the third order  $\Lambda_i$ . The

<sup>\*</sup> Because of the reflection symmetry of the nucleus, the wave function (3) has to be symmetrized correspondingly<sup>2</sup>. However, for our purposes we can use the nonsymmetric expression.

linear term of its expansion in wave vectors of the external field  $q/\frac{1}{h}$  has the following form  $[(\hat{q} = q_{\alpha}\gamma_{\alpha}; q \simeq (q; iq_0)]:$ 

$$\Lambda_i = (\pi^2 / 2m) F(\gamma_i \hat{q} - \hat{q} \gamma_i).$$
 (1)

The coefficient F serves to specify the radiative correction to the magnetic moment, i.e.,

$$\Delta \mu / \mu = (\alpha / 2\pi) F.$$
 (2)

For  $|\lambda_0| = \infty$ , we have F = 1, and Eq. (2) is just the Schwinger formula. For finite  $\lambda_0$ , we can write  $F = 1 - \delta F(\lambda_0)$ , and hence

$$\Delta \mu / \mu = (\alpha / 2\pi) \left[ 1 - \delta F(\lambda_0) \right]. \tag{3}$$

F is expressed by integrals in momentum space of the form

$$J = \int \frac{d^4k \, [1; \, k_{\sigma}; \, k_{\sigma}k_{\tau}]}{(k^2 - 2p_1k) \, (k^2 - 2p_2k) \, k^2} \quad .$$

 $(p_1 \text{ and } p_2 \text{ are the initial and final momenta of the meson and <math>p_2 - p_1 = q$ ). Instead of integrating over a finite region one can retain the infinite integration limits and introduce Feynman's<sup>3</sup> truncating factor  $\lambda_0^2/\lambda_0^2 + k^2$ . Then

$$J(\lambda_0) = J(\infty) - \delta J(\lambda_0),$$

where

$$\delta J(\lambda_0) = \int \frac{d^4k \, [1; \, k_{\sigma}; \, k_{\sigma}k_{\tau}]}{(k^2 - 2p_1 k) \, (k^2 - 2p_2 k) \, (k^2 + \lambda^2)} \, .$$

Continuing the calculation in the usual manner<sup>3,4</sup>, we obtain for the apex the following expression

$$\Lambda_{i}(\lambda_{0}) = \Lambda_{i}(\infty) - \delta\Lambda_{i}(\lambda_{0});$$

$$\delta \Lambda_i(\lambda_0) = \int_0^1 2x \, dx \int_0^1 dy \, \{(1 - y - xy) \, \hat{q} \gamma_i - (1 - x + xy) \, \gamma_i \hat{q} \}$$

 $\times \frac{\pi^2 m x}{x^2 p_y^2 - (1 - x) \lambda_0^2}, \quad (4)$ 

where

$$p_y = yp_1 + (1 - y)p_2.$$

Let us first perform the integration over  $\gamma$ . Since we are only interested in terms linear in q, we can substitute  $p^2 = -m^2$  for  $p_{\gamma}^2$  in the integrand. Then Eq. (4) assumes the form of Eq. (1), viz.,

$$\delta\Lambda_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} - \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i} = (\pi^{2} / 2m) \left(\gamma_{i} \hat{q} \gamma_{i}\right) \delta F(\lambda_{0}), \quad \mathcal{A}_{i$$

where

$$\delta F(\lambda_0) = 2 \int_0^{\infty} \frac{(1-x) x^2}{x^2 + (\lambda_0 / m)^2 (1-x)} dx$$
(5)  
= 1 + 2\gamma - \gamma (\gamma + 2) \ln \frac{1}{\gamma}  
- \frac{\gamma^2 + 4\gamma + 2}{V \frac{1}{1+4} / \gamma} \ln \frac{1 + V \frac{1}{1+4} / \gamma}{1 - V \frac{1}{1+4} / \gamma} \ln \frac{1}{1 - V \frac{1}{1+4} / \gamma} \ln \frac{1}{1+4} / \frac{1}{1+4} / \frac{1}{1+4} / \gamma} \ln \frac{1}{1+4} / \frac{1}{1

 $(\gamma = \lambda_0^2/m^2)$ . With  $\gamma \gg 1$ , the value of the integral is

$$\delta F(\lambda_0) = 2m^2 / 3\lambda_0^2. \tag{6}$$

<sup>1</sup> L. Landau and I. Pomeranchuk, Dokl. Akad. Nauk SSSR 102, 489 (1955); I. Pomeranchuk, Dokl. Akad. Nauk SSSR 103, 1005 (1955); Dokl. Akad. Nauk SSSR 104, 51 (1955).

<sup>2</sup> G. Gandel'man and Ia. Zel'dovich, Dokl. Akad. Nauk SSSR 105, 445 (1955).

<sup>3</sup> R. Feynman, Phys. Rev. **76**, 769 (1949).

<sup>4</sup> A. Akhiezer and V. Berestetskii, *Quantum Electro*dynamics, Moscow, 1953.

Translated by A. Skumanich 158

## Charged Particle Green's Function in the "Infrared Catastrophe" Region

L. P. Gor'kov

Institute for Physical Problems Academy of Sciences, USSR (Submitted to JETP editor January 3, 1956) J. Exptl. Theoret. Phys. (U.S.S.R.) 30, 790-791 (April, 1956)

IN the electrodynamics of the electron Abrikosov<sup>1</sup> has shown that the interaction with the electric field leads to the appearance in the Green's function of the electron in the infrared region  $(|p^2 - m^2| \ll m^2)$  of the additional singularity

$$\left(\frac{m^2}{p^2 - m^2}\right)^{(e^3/2\pi) [3 - d_l(0)]} \tag{1}$$

as compared with the simple pole for the Green's function of the free electron. An analogous investigation in the electrodynamics of spin zero<sup>2</sup>